



DISPEC

Scientific exploitation of space Data for improved Ionospheric SPECification

SDA2 : "Modeling Trans-ionospheric Radio Signal Propagation"

Fabbro Vincent , Xavier Bauman (ONERA) & DISPEC team

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SDA2. Modeling Trans-ionospheric Radio Signal Propagation

Context

- The need for modeling radio signal propagation through the ionosphere **remains high** and is becoming more **challenging** due to new requirements for **accuracy** and **rapid availability**.
- Further investigation into the ionosphere's complexity and dynamics requires unprecedented detail to **evaluate plasma irregularity effects**.
- Modeling signal propagation is extremely complex and demands **high computational performance**, especially when the ionosphere is considered as an anisotropic, inhomogeneous plasma without simplifications (or neglecting the Earth magnetic field).

SDA2. Modeling Trans-ionospheric Radio Signal Propagation

Context

- Ionospheric medium characterization : IRTAM / NeQuick / IRI

Assimilative IRTAM 3D (IRI-based Real-Time Assimilative Model).

[Galkin et al., 2022]

uses real-time measurement feeds from GIRO (Global Ionosphere Radio Observatory)

Note : A python version pyIRTAM exists available on GitHub

[Forsythe et al., 2024]

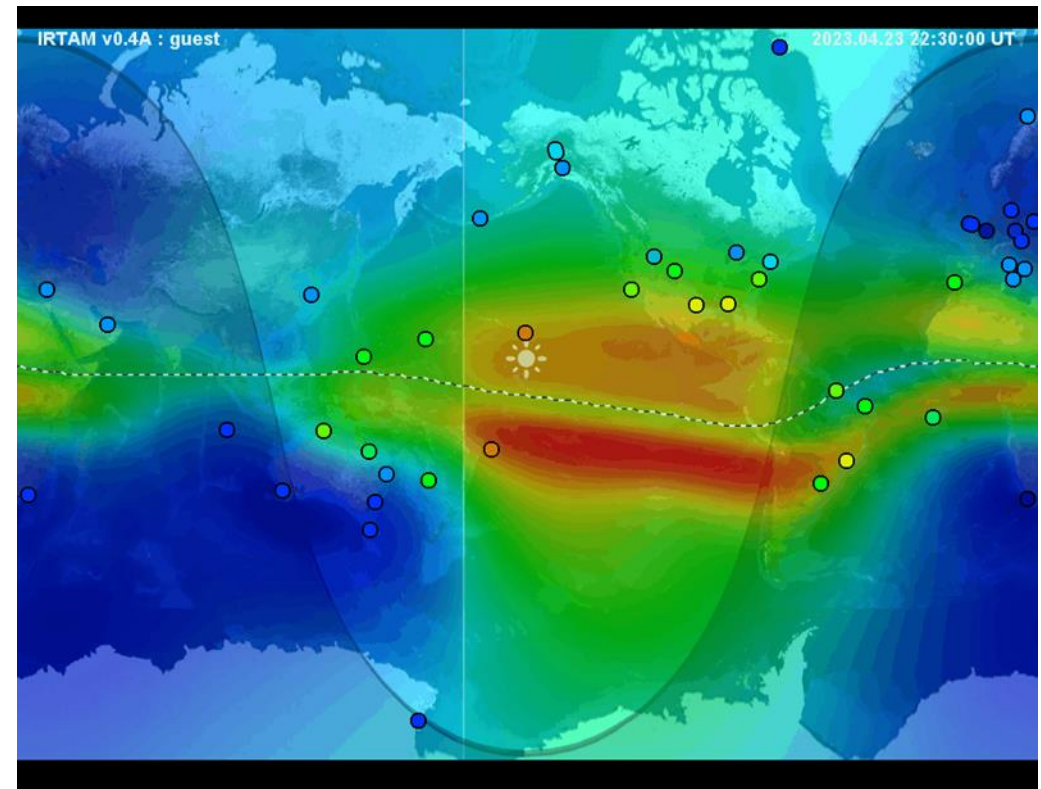


Figure: Illustration of IRTAM 3D results obtained using the GAMBIT tool.

SDA2. Modeling Trans-ionospheric Radio Signal Propagation

- Propagation modeling : **Haselgrove equation resolution model**

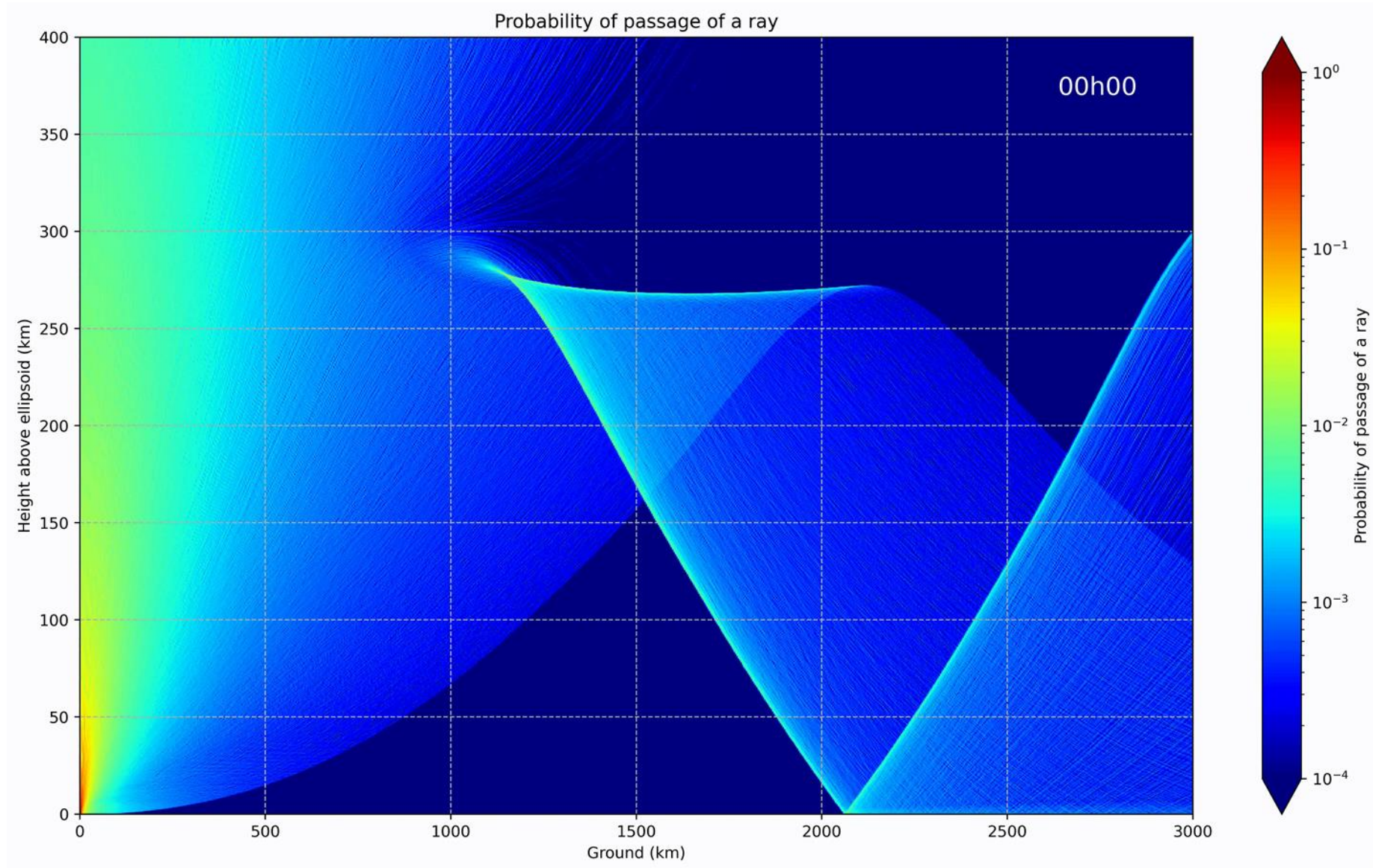
- **Basic principle:** **Hamiltonian** formulation of the wave equation -> **coupled equation** systems giving the **trajectory** and **wave vector** of the wave at each point of the trajectory.
- **Initial parameters:** frequency, azimuth, elevation -> require a search method to reach the receiver.
- **Numerical resolution methods:** Runge-Kutta-4 or Runge-Kutta-Dormand-Prince to better control the integration error.
- **Limitation:** Assume a slow variation of the ionosphere -> unsuitable for studying short-lived phenomena such as bubbles.

$$H = \frac{1}{2} \Re \left[\left(\frac{c}{\omega} \right)^2 (k_r^2 + k_\theta^2 + k_\varphi^2) - n^2 \right]$$

$$\left\{ \begin{array}{l} \frac{dr}{dP} = -\frac{1}{c} \frac{dH}{dk_r} / \frac{dH}{d\omega} \\ \frac{d\theta}{dP} = -\frac{1}{rc} \frac{dH}{dk_\theta} / \frac{dH}{d\omega} \\ \frac{d\varphi}{dP} = -\frac{1}{rc \sin(\theta)} \frac{dH}{dk_\varphi} / \frac{dH}{d\omega} \end{array} \right.$$

$$\left\{ \begin{array}{l} \frac{dk_r}{dP} = \frac{1}{c} \frac{dH}{dr} / \frac{dH}{d\omega} + k_\theta \frac{d\theta}{dP} k_\varphi \sin(\theta) \frac{d\varphi}{dP} \\ \frac{dk_\theta}{dP} = \frac{1}{r} \left(\frac{1}{c} \frac{dH}{d\theta} / \frac{dH}{d\omega} - k_\theta \frac{dr}{dP} + k_\varphi r \cos(\theta) \frac{d\varphi}{dP} \right) \\ \frac{dk_\varphi}{dP} = \frac{1}{r \sin(\theta)} \left(\frac{1}{c} \frac{dH}{d\varphi} / \frac{dH}{d\omega} - k_\varphi \sin(\theta) \frac{dr}{dP} - k_\varphi r \cos(\theta) \frac{d\theta}{dP} \right) \end{array} \right.$$

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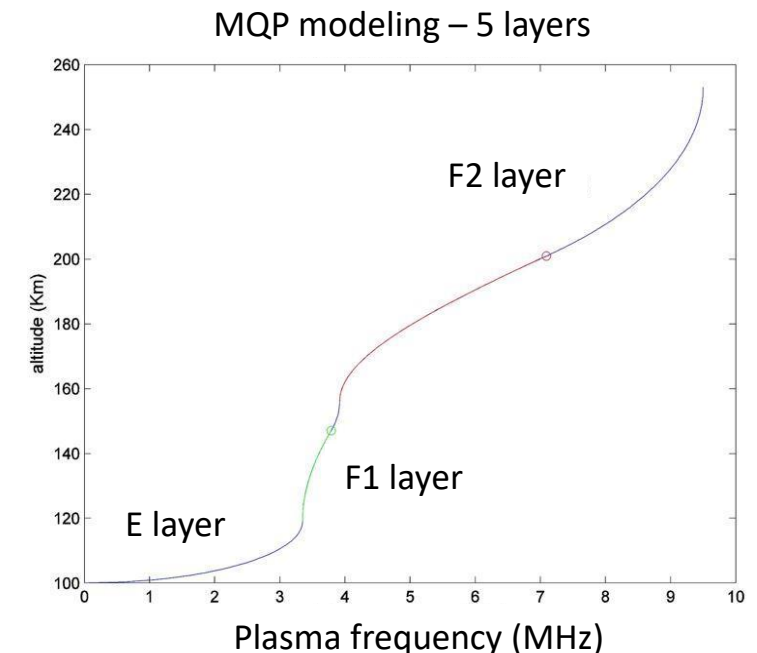


SDA2. Modeling Trans-ionospheric Radio Signal Propagation

- Propagation modeling : **MQP model (Multi Quasi Parabolic)**

- Basic principle:** Description of vertical ionospheric density profile by **segments of quasi-parabola**. Then, **analytic formulations available** to compute the ray trajectory (i.e. **group distance**).
- Initial parameters:** frequency, azimuth, elevation -> require a search method to reach the receiver.
- Limitations:**
 - Approximation of electron density profile by MQP
 - No variability of the profile vs distance, nor lateral dimension
 - Assumes approximation of the refractive index

$$f(r)^2 = f_{Pi}^2 \left[1 \mp \frac{(r - r_{mi})^2}{y_{mi}^2} \frac{r_{bi}^2}{r^2} \right]$$

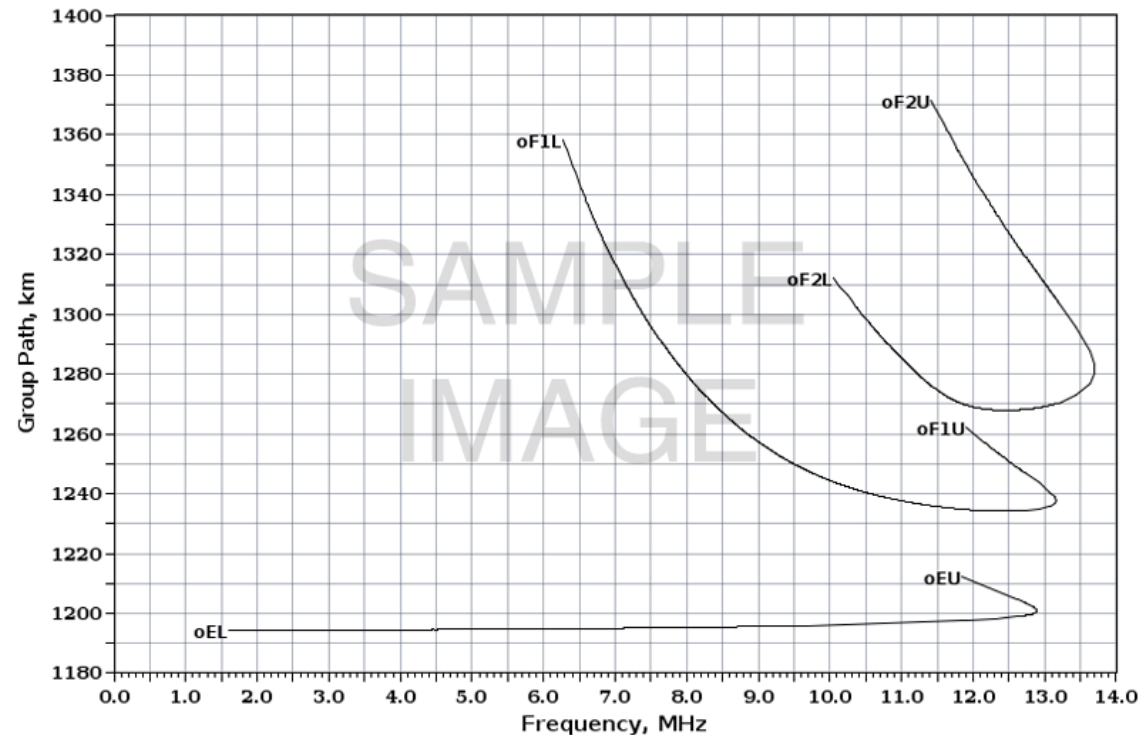


SDA2. Modeling Trans-ionospheric Radio Signal Propagation

- Propagation modeling : **MQP model (Multi Quasi Parabolic)**

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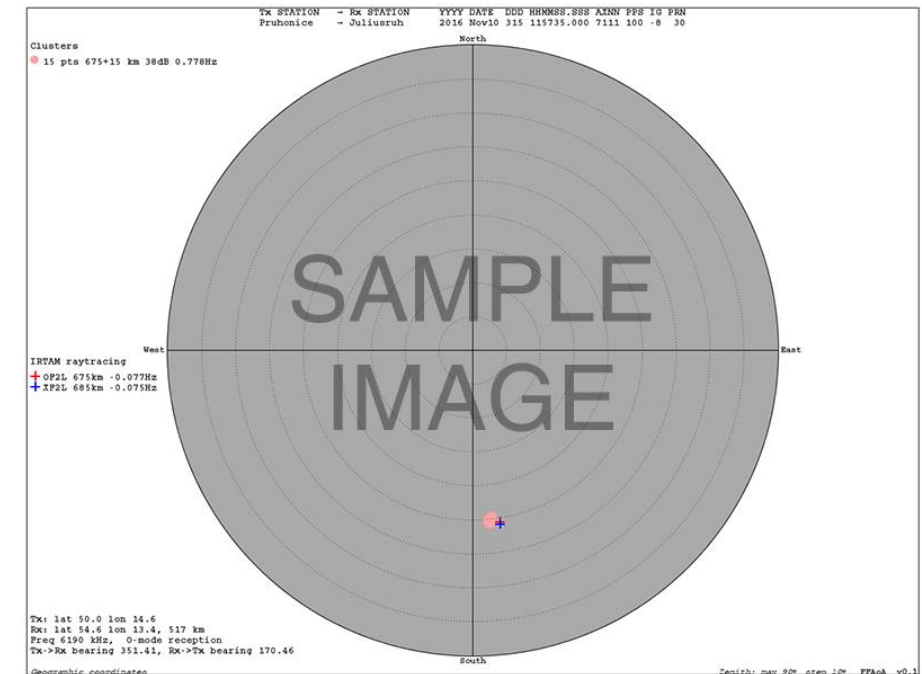


RayTRIX-CQPSynth 0.1B

This service uses a spherically stratified Composite-Q DP is matched to the Assimilative IRI profile at the midpoint, calculated using near-real-time GIRO data.



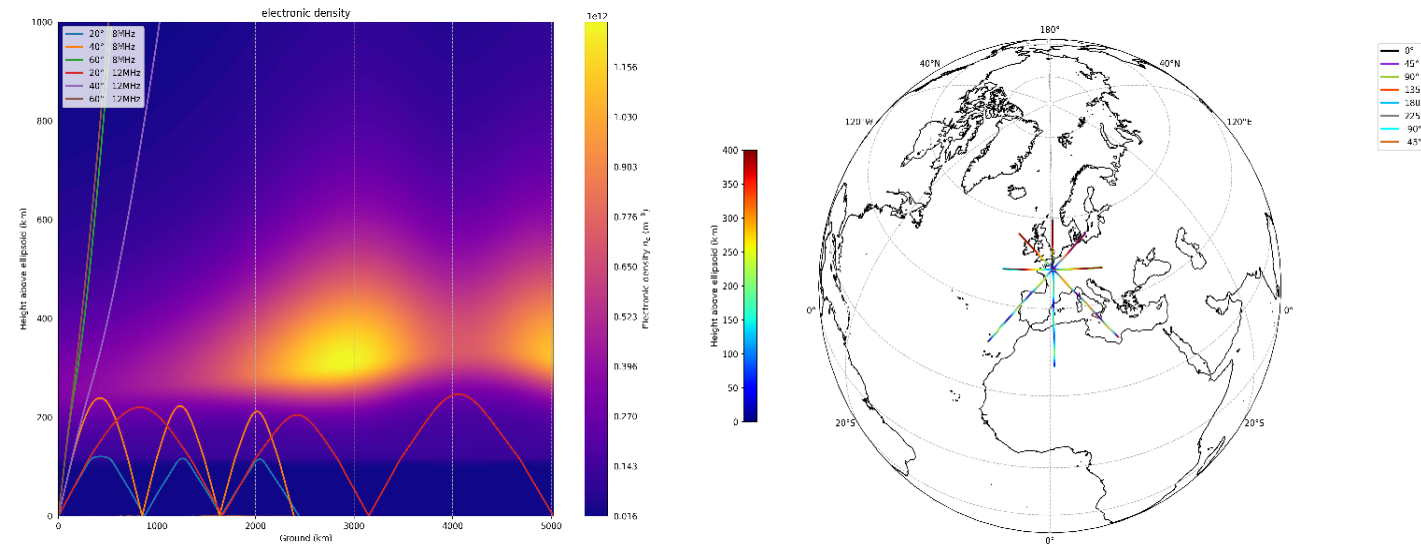
<https://giro.uml.edu/rix/oi-synth/>



SDA2. Modeling Trans-ionospheric Radio Signal Propagation

- Review of Scientific models underpinning SDA2 (regarding their operational capability)
 - 1. LIMPID-HF 3D raytracer with quiet-time background ionosphere modeled by NeQuick or IRI,

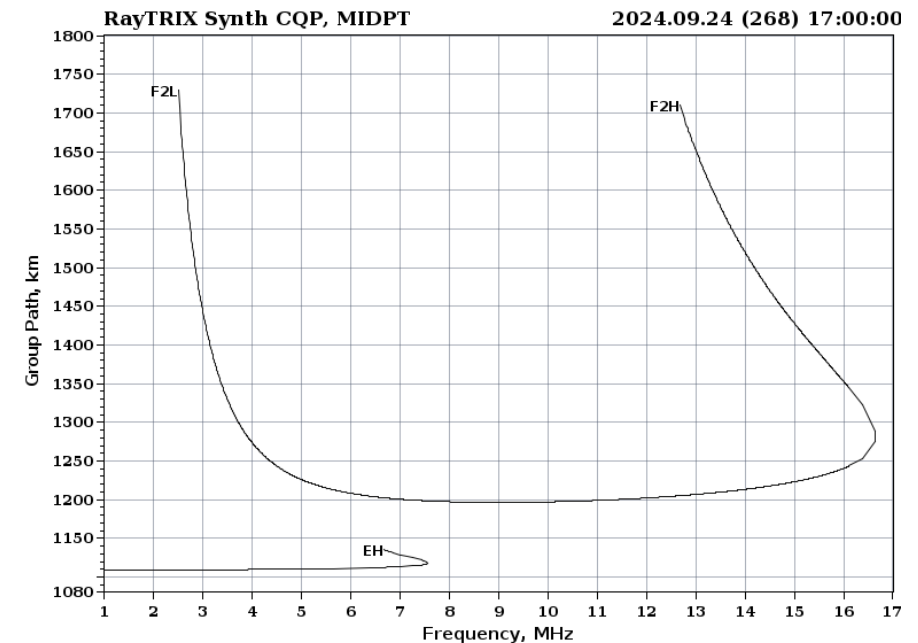
Ionosphere modeled by NeQuick or IRI
resolution of Haselgrove equations (3D)



SDA2. Modeling Trans-ionospheric Radio Signal Propagation

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 1. LIMPID-HF 3D raytracer with quiet-time background ionosphere modeled by NeQuick or IRI,
 2. RayTRIX CQP (Composite Quasi-Parabolic), extended to 2 hops

Simplified electron density profile and propagation
Based on IRTAM background ionosphere
IRI is also possible



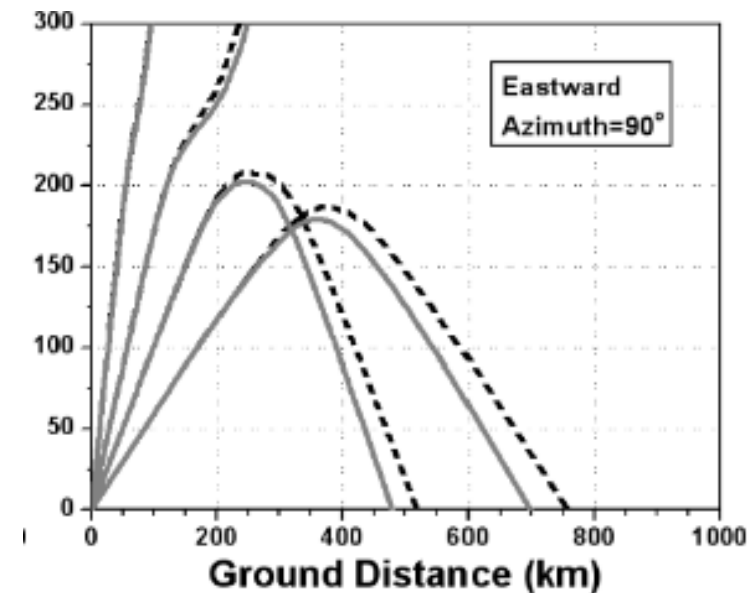
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RixCore 0.5

SDA2. Modeling Trans-ionospheric Radio Signal Propagation

- Review of Scientific models underpinning SDA2 (regarding their operational capability)
 1. LIMPID-HF 3D raytracer with quiet-time background ionosphere modeled by NeQuick or IRI,
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 3. HR2006 Numerical 3D raytracer (Parallelized and rewritten in GPU) with IRTAM background ionosphere

IRI-like profile formalism for background ionosphere
IRTAM is possible
Overlaying TIDs is also possible



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Outputs: synthesized Doppler skymaps and oblique ionograms
- Tests to verify the results:
 - ✓ Validations : (1) vs (2) vs (3) on quiet-time background ionosphere (and no Earth magnetic field, neither collision profile), with 1 or 2 hops
 - ✓ Validations : (1) vs (2) vs (3) on quiet-time background ionosphere, with Earth magnetic field
 - ✓ (1) (2) (3) : **Cross-validation** versus **D2D oblique** sounding **data**
(2) and (3) should demonstrate improved performance with **DISPEC high-level data products**

Thank you for your attention!

WEB: <https://dispec.eu>



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